

STA 303 / 1002

GAS for mixed:Uses Restricted maximum likelihood to estimate

model parameters: - covariance parameters - using MLE  
- coefficients of fixed effects - ( $\beta$ 's)  
- generalized least squares

Since covariances & variances are estimated using ML,  
can compare models with same  $Y$  same  $X$ 's but  
different covariances structures using AIC, SC = BIC

or LRTs

(Bayesian Information Criterion)

$$AIC = -2 \log L + 2 (\# \text{ of covariance parameters})$$

$$BIC = -2 \log L + (\# \text{ of covariance parameters}) \log(n)$$

where  $n = \#$  of subjects

- smaller is better

Since  $\beta$ 's are estimated by generalized least squares, tests and CI's for  $\beta$ 's, use  $t$  and  $F$ -tests

Example From Type 3 Tests of Fixed Effects

$\rightarrow$   $p$ -value for diet \* time interaction: 0.0162

So we have evidence that difference among diets differs

answer times in mean HDL  
(we'll follow up with more details later)

Does assumed variance-covariance structure seem reasonable?

Looking at variance est by diet (from prev con by diet),  
some indication that variability of HDL measurements is less,  
on diet L6 (s.d.  $\sim 2$  on L6 but  $\sim 3$  on other diets)  
Seems reasonable to assume that correlations are the same.

Can fit model with more complicated covariance  
structure than compound symmetry using repeated statement

Will use: type = UN  
 ↳ unstructured  
 ↳ all variances and covariances estimated from data  
 ↳ of covariance structure

group option - different variance-covariance matrix for subjects depending on subject  
 (none have to)

For 3 measurements on subject with diet H<sub>g</sub>

$$D_{H_g} = \begin{pmatrix} \sigma_{1, H_g}^2 & \sigma_{12, H_g}^2 & \sigma_{13, H_g}^2 \\ \sigma_{12, H_g}^2 & \sigma_{2, H_g}^2 & \sigma_{23, H_g}^2 \\ \sigma_{13, H_g}^2 & \sigma_{23, H_g}^2 & \sigma_{3, H_g}^2 \end{pmatrix}$$

where  $\sigma_{i, H_6}^2$  is var. of observations at time  $i$  for subject on diet  $H_6$   
 $\sigma_{12, H_6}^2$  is cov. of observations between times 1 & 2 for subject on diet  $H_6$ ,  
etc.

For diet  $H_6$ : 6 covariance parameters to estimate  
(3 var + 3 cov)

$\Rightarrow$  Total of 18 covariance parameters for all 3 diets

Example!

For disk  $H_9$

$$\hat{D}_{H_9} = \begin{pmatrix} .1190 & .1080 & .1029 \\ .1080 & .1168 & .1073 \\ .1029 & .1073 & .1029 \end{pmatrix}$$

$$\hat{D}_{HM} = \begin{pmatrix} .1064 & & \\ .1002 & .1281 & \\ .1156 & .1315 & .1494 \end{pmatrix}$$

$$\hat{D}_{L_6} = \begin{pmatrix} .03427 & & \\ .04201 & .04101 & \\ .03482 & .03647 & .04470 \end{pmatrix}$$